MULTICRITERIA DECISION MAKING

Business Decision Making

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THE **STRUCTURE**

Context

Basics





The context of the topic

A. Multi-criteria decision making (MCDM)

SAW - simple additive weighting

Foundations of the pairwise comparisons method

- A. Saaty scale
- B. Transitivity concept

Pairwise comparisons procedure

- A. Calculating the weights/priorities
- B. Calcualting the inconsistency in giving judgements

Using the PC procedure

- A. Methods (AHP)
- B. Applications

THE **CONTEXT** OF THE TOPIC

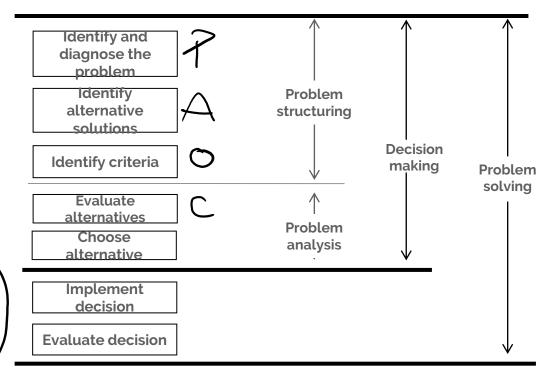
PrDAC(Tapproach: decomposition od DM problem into

elements

Basic elements:
 Problem, Objectives (criteria, attributes),
 Alternatives,
 Consequences and

Tradeoffs -

Elements for decision making in turbulent environment: Risk tolerance, Uncertainty, Linked decisions



THE CONTEXT OF THE TOPIC

- Two decision-making methods groups
 - Methods that support multicriteria decision making (basic PrOACT elements)
 - Methods that support decision making under uncertainty and risk (PrOACT elements for decision making in turbulent environment)
- Multi-criteria decision-making (MCDM)
 - Decomposition of the main decision-making goal into several sub goals that are described with criteria (attributes)
 - The MCDM problems can be easily described by using the table od values (matrix of decision-making)
 - Alternatives (3), Criteria (3), Consequences/Values (9)

| Candidate 2 Secondary s 0 years 6 | | Education | Experience | CV |
|------------------------------------|-------------|--------------|------------|----|
| | Candidate 1 | High | 5 years | 5 |
| Canadialata | Candidate 2 | Secondary s | o years | 6 |
| Candidate 3 Secondary s. 2 years / | Candidate 3 | Secondary s. | 2 years | 7 |



THE **CONTEXT** OF THE TOPIC

Multicriteria decision making is ... about criteria

• Criteria = attributes

Types of the criteria:

- Qualitative (words): color, design, ...
- Quantitative (numbers): price, weights, height ... two subtypes:
 - Min criteria (criteria of costs): price (when we buy), fuel consumption, ...
 - Max criteria (criteria of benefits): price (when we sell), quality, ...
- Types of the criteria 2:
 - Natural price, consumption, ...
 - Constructed scale measuring the properties on some scale
 - Proxy criteria quality of life is measured with GDP



Context

Basics

Procedure

Usage

Multi-criteria decision making

| | (| Time | Cost | Satisf. |
|------|---|------|--------|------------------------|
| Make | | 100 | 50 | High |
| Buy | | 10 | 150 | High |
| SQ / | | 0 | 0 | OK |
| | | Make | Buy 10 | Make 100 50 Buy 10 150 |

| / | | Time | Cost | Satisf. | TP | \ |
|---|----|------|------|---------|----|---|
| • | | | | | | |
| • | М | | | | | |
| | В | | | | | |
| • | ZQ | | | | | |
| | | | | | | |

- Table of decision making: alternatives, criteria and consequences
- Methods: Evenswaps, Electra, Promethee, Topsis (AHP) Dex method, VIKOR, WINGS, SNAP...
- The results:
 - Criteria weights
 - Local priorities of the alternatives per each criterion
 - Total priorities of the alternative DECISION!



Simple additive weighting (SAW)

| | Time | Cost | Satisf. |
|------|------|------|---------|
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ | 0 | 0 | OK |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | | | | |
| М | | | | |
| В | | | | |
| SQ | | | | |

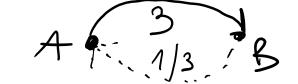
- Criteria weights (. 5 procedures

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Total priorities of the alternativa

$$\oint \hat{s}_i = w_1 r_{i1} + w_2 r_{i2} + \dots + w_m r_{im} = \sum_{k=1}^m w_k r_{ik}$$

Basics



THE BASIC FOUNDATIONS OF THE TOPIC

Saaty's scale

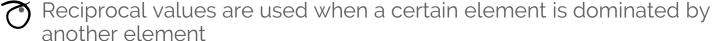
• Founder: prof. Thomas Saaty

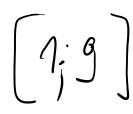
It describes the relation between two elements

Values of the scale:

• 1 = Two elements are equally important

- 3 = Weak importance of one element over another
- 5 = Strong importance of one element over another
- 7 = Demonstrated importance of one element over another
- 9 = Absolute importance of one element over another
- All real values from scale [1;9] can be used





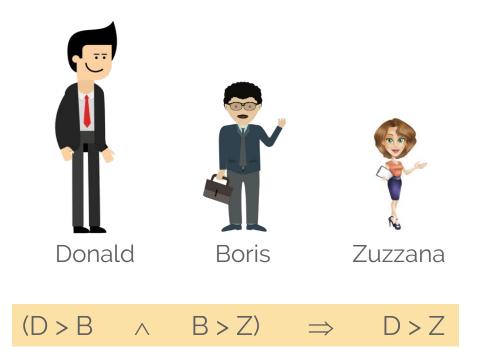








Transitivity concept (math)

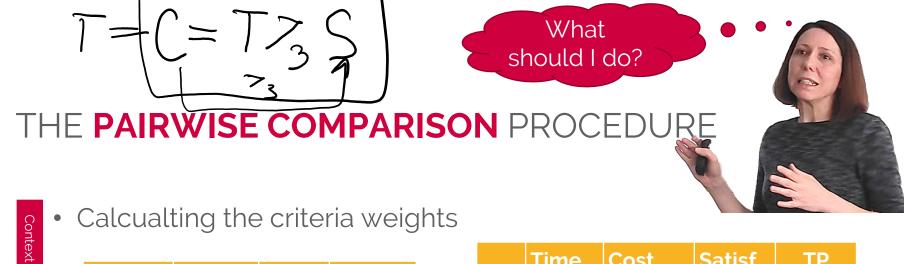


Transitivity concept (math) + Saaty's scale

Donald Boris Zuzzana

IN/CONSISTENCY

 $(D >_3 B \land B >_2 Z) \Rightarrow D >_5 Z$



| | Time | Cost | Satisf. | |
|------|------|------|---------|--|
| Make | 100 | 50 | High | |
| Buy | 10 | 150 | High | |
| SQ | 0 | 0 | OK | |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | 0.43 | 0.43 | 0.14 | |
| М | | | | |
| В | | | | |
| SQ | | | | |

0.43

0.43

0.14

0.43

0.14

| | W | | | | | 1 | 2.3 |
|----------|----|-----|-----|-----|-----|------|-----|
| | | | T/ | С | S. | 3.3 | 7 |
| | | T. | 1 | 1 | (3) | 0.43 | 0.4 |
| ' | fr | С | 1 | 1 | 3 | 0.43 | 0.4 |
| | | S | 1/3 | 1/3 | 1 | 0.14 | 0.1 |
| | | SUM | 2.3 | 2.3 | 7 | ~ | Ax |
| | | | | | | | |

IN/CONSISTENCY

Input: PC matrix
Output: CR ←

CR<0.1

<u>Additional reading</u>



Procedure



THE PAIRWISE COMPARISON PROCEDURE

Calculate the alternatives' priorities (for each column)

| | Time | Cost | Satisf. |
|------|------|------|---------|
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ | 0 | 0 | OK |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | 0.43 | 0.43 | 0.14 | |
| M | | | | |
| В | | | | |
| SQ | | | | |

Repeat the procedure three times – 3 columns of local priorities!

Procedure

What should I do?

THE **PAIRWISE COMPARISON** PROCEDURE

Calculate the alternatives' priorities (for each column)

| | | \ | |
|------|------|------|---------|
| | Time | Cost | Satisf. |
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ (| 0) | 0 | OK |
| | _ / | | |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | 0.43 | 0.43 | 0.14 | |
| M | | | | |
| В | | | | |
| SQ | | | | |

| Time | М | В | SQ |
|------|------------|------|------|
| М | 1 | 1/3 | 1/5 |
| В | 3 | 1 | 1/3 |
| SQ | <u>(5)</u> | 3) | 1 |
| SUM | 9 | 4,33 | 1,53 |

| 0.11 | 0.08 | 0.13 | 0.11 |
|------|------|------|------|
| 0.33 | 0.23 | 0.22 | 0.26 |
| 0.55 | 0.69 | 0.65 | 0.63 |
| | | | |



Context

Procedure

THE PAIRWISE COMPARISON PROCEDURE

Calculate the alternatives' priorities (for each column)

| | Time | Cost | Satisf. |
|------|------|------|---------|
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ | 0 | 0 | OK |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | 0.43 | 0.43 | 0.14 | |
| М | 0.11 | | | |
| В | 0.26 | | | |
| SQ | 0.63 | | | |

| Cost | М | В | SQ |
|------|------|---|-----|
| М | 1 | 3 | 1/2 |
| В | 1/3 | 1 | 1/5 |
| SQ | 2 | 5 | 1 |
| SUM | 3.33 | 9 | 1.7 |

| 0.3 | 0.33 | 0.29 | 0.31 |
|-----|------|------|------|
| 0.1 | 0.11 | 0.18 | 0.11 |
| 0.6 | 0.55 | 0.58 | 0.58 |

THE **PAIRWISE COMPARISON** PROCEDURE

Calculate the alternatives' priorities (for each column)

| | Time | Cost | Satisf. |
|------|------|------|---------|
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ | 0 | 0 | OK |

| | Time | Cost | Satisf. | TP |
|----|------|------|---------|----|
| | 0.43 | 0.43 | 0.14 | |
| М | 0.11 | 0.31 | | |
| В | 0.26 | 0.11 | | |
| SQ | 0.63 | 0.58 | | |

| Satis. | М | В | SQ |
|--------|------|------|----|
| М | 1 | 1 | 4 |
| В | 1 | 1 | 4 |
| SQ | 1/4 | 1/4 | 1 |
| SLIM | 2.25 | 2.25 | 0 |

| 0.44 | 0.44 | 0.44 | 0.44 |
|------|------|------|------|
| 0.44 | 0.44 | 0.44 | 0.44 |
| 0.12 | 0.12 | 0.12 | 0.12 |

| SUM | 2.25 | 2.25 | 9 |
|-----|------|------|---|
| | | | |

THE PAIRWISE COMPARISON PRO

Agretating the criteria weights and local priorities in SAW,

| | Time | Cost | Satisf. |
|------|------|------|---------|
| Make | 100 | 50 | High |
| Buy | 10 | 150 | High |
| SQ | 0 | 0 | OK |

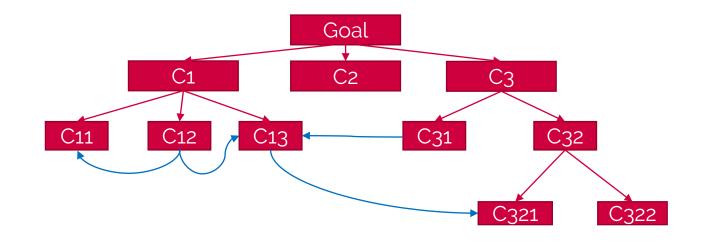
| | Time | Cost | Satisf. | TP |
|----|------|------|---------|------|
| | 0.43 | 0.43 | 0.14 | |
| М | 0.11 | 0.31 | 0.44 | 0.24 |
| В | 0.26 | 0.11 | 0.44 | 0.22 |
| SQ | 0.63 | 0.58 | 0.22 | 0.54 |

Calculating the total priorities:

$$\varsigma_i = w_1 r_{i1} + w_2 r_{i2} + \dots + w_m r_{im} = \sum_{k=1}^{n} w_k r_{ik}$$

Methods

- SIMPLE ADDITIVE WEIGHTING (SAW)
- ANALYTIC HIERARCHY PROCESS (AHP)
- ANALYTIC NETWORK PROCESS (ANP)

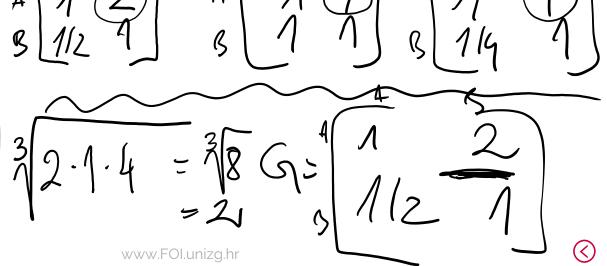


AHP

- The Analytic Hierarchy Process (AHP) (Saaty, 1980) is well known multicriteria decision-making method
- The AHP is a powerful and flexible decision-making method which helps people to set priorities and make the best decision when both qualitative and quantitative aspects of a decision need to be considered.

The AHP can combine judgments into a single representative judgment for the group and also including the importance of the individuals





THE **USAGE** OF THE PAIRWISE COMPARISONS

AHP

Context

Procedure

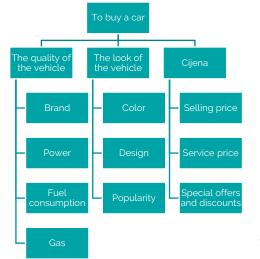
Usage

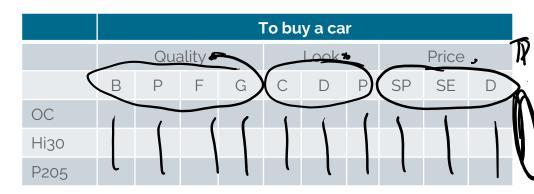
• It is a more complex variant of the SAW method and PC method – the decision-making problem is more complex

In the AHP, the criteria are not placed on to one level only – there is a hierarchy structure which is more complex

| | Price | Fuel | Color |
|----|-------|------|-------|
| A1 | 50000 | 6 | Blue |
| A2 | 55000 | 5 | Red |
| A3 | 56000 | 5 | Black |

| | | ` | | | / \ | ١ . | / | | \ |
|---|-----|-------|-------|------|------|-------|-------|------------|---|
| | SAW | Price | 0,571 | FC (| ,286 | Coloi | 0,147 | 7 P | |
| | A1 | 0,540 | | 0,2 | | 0,163 | 1 | | |
| ク | A2 | 0,297 | | 0,4 | | 0,297 | | | |
| | A3 | 0,163 | 1 | 0,4 | | 0,540 | 1 | | |
| | | | | | | | | | |





THE **USAGE** OF THE PAIRWISE COMPARISONS

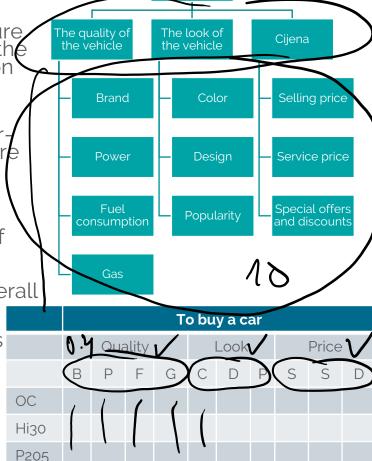
AHP - steps

1. The AHP enables decision makers to structure decisions hierarchically. The overall goal of the decision is at the top of the model, evaluation criteria in the middle levels, and alternative choices at the bottom

2. Decision makers begin the procedure of pairwise comparisons on each hierarchy structure level in order to determine the relative importance of elements on each level

On the basis of the pair-wise comparisons, relative significance (weights) of elements of the hierarchy structure are calculated (calculation of relative priorities for criteria), which are eventually synthesized into an overall priority list of alternatives (inconsistency)

4. The sensitivity analysis. Sensitivity analysis is used to determine how the priorities of the alternatives change with respect to the importance of the criteria.



To buy a car

Context

Basics

Procedure

Usage

THE **USAGE** OF THE PAIRWISE COMPARISONS

Applications

- Ranking the hospitals in Croatia
- Planning the traffic in Croatia
- Smooth vehicular flow and safe pedestrian crossing separately (Sri Lanka)
- Garage-parking Facility Location Selection in Croatia
- **Planning the traffic safety in Turkey**
- Selecting the flight procedure design schemes in China
- Prioritisation of the safety control criteria in maritime traffic
- **Evaluation Framework for Key Performance Indicators of Railway ITS**





ASSIGNMENT 1 PC

Decision-making table

| | Price | Brand | Engine | Fuel comsumtion | Color |
|----|-------|---------|------------|-----------------|-------|
| A1 | 50000 | Opel | 1.8 diesel | 6 | Blue |
| A2 | 55000 | Peugeot | 2.2 diesel | 5 | Red |
| А3 | 56000 | BMW | 2.5 diesel | 8 | Black |

- Calculate the criteria weights using the PC procedure
- Calculate the local priorities of the alternatives using the PC procedure
- Calculate the total priorities of the alternatives



ASSIGNMENT 2 AHP

- Choose any strategic MCDM problem you want (it can be personal, business etc.) and describe it.
- Define criteria relevant for the problem and present them through the hierarchy (at least 2 levels of the criteria, at least 3 criteria at the first level and at least 12 not-decomposed criteria). Describe the criteria.
- Define at least three alternatives and describe them.
- Make decision making table
- Calculate the weights of the criteria, subcriteria and priorities of the alternatives as well as the total priorities. Calculate the inconsistency ratio for each pairwise comparison table.
- Make the sensitivity analysis changing the weights of each criterion on the first level +/-5% and calculating the total priorities of the alternatives in each change. Make cummulative table. Ex. If you have 3 criteria, you will have 6 sensitivity analyses (each criterion +5%, each criterion -5%). In cummulative table for each sensitivity analysis you have to determine if the firstly ranked alternative stayed first or not.
- Make final decision.
- Make word document. 4000 words. You can use Excel to speedup the calculation procedure.